**BIRLA INSTITUTE OF TECHNOLOGY AND SCIENCE, PILANI-HYDERABAD CAMPUS SECOND SEMESTER 2022–2023**

**COURSE HANDOUT**

*Date : 16.1.2023*

In addition to Part I (General Handout for all courses appended to the Time Table), this portion gives further specific details regarding the course.

**Course No. :** PHY F243

**Course Title :** Methods of Mathematical Physics I

**Instructor-in-charge :** Swastik Bhattacharya

**Instructor :** Swastik Bhattacharya

# Course Description :

This course deals with some of the mathematical methods which are used in many branches of theoretical physics.

# Scope and Objective :

MMP I is a course on mathematical methods used in physics. The emphasis will be on understanding the general principles and on methods which have not been covered in the various core Mathematics courses which the student has already undergone. Applications cover a wide range of physical problems.

# Text Books:

T1: Mathematical Methods for Physicists: Arfken, Weber, Harris, 7th edition, Academic Press, 2012.

T2: Mathematics for Physicists: Philippe Dennery, Andre Krzywicki, Dover Books on Physics, Dover Publications Inc, 1996

# Reference Books:

R1: Tensor Analysis, Schaum’s outline on theory and problems of tensor calculus. Tata Mcgraw Hill.

R2: Introduction to Vector Spaces in Physics, K.A.I.L. Wijewardena Gamalath, Cambridge University Press

Notes to be provided by the instructor

# Course Plan:

Sections referred to are from the text book unless stated otherwise.

|  |  |  |  |
| --- | --- | --- | --- |
| Lecture No. | Learning Objectives | Topics to be Covered | Reference |
| 1 | Discussion of the objectives of the course  and the approach to be followed |  |  |
| 2-7 | Complex Analysis | Stereographic projection, Analytic  functions, Cauchy’s theorem, Jordan’s lemma, Evaluation of | T1:  Chapter 11, Notes |

|  |  |  |  |
| --- | --- | --- | --- |
|  |  | integrals, gamma function |  |
| 8-12 | Fourier Transform | Definition and Properties of Fourier Transform, Convolution Theorem and Applications | T1  Chapter 20, T2,  Notes |
| 13-17 | Partial Differential equations | Examples of PDEs: Continuity equation, diffusion equation, Wave equation, Poisson and Laplace  equation, Seperation of Variables, Boundary conditions. | T1  Chapter 9. T2 |
| 18-21 | Green’s functions | Motivation and Introduction to Green’s Functions, Green’s Identity, Adjoint Boundary conditions, 2nd order self-adjoint operators and Green’s functions, properties, construction and uniqueness, Generalised Green’s Functions, 2nd order ODEs with inhomogeneous boundary conditions, Sturm- Liouville problem, Eigenfunction  expansion of Green’s functions | T2, T1  Chapter 10 |
| 22-30 | Matrices, Vector Spaces, Linear Operators. | Matrix Properties, Levi Civita symbol, Hermitian, Orthogonal Matrices, Vector spaces, Norms and Inner products, Gram Schmidt  Orthogonalisation, Similarity transformations, diagonalisation | T1  Chapter 1,2,3,4 of R3 |
| 31-34 | Tensors and Differential Geometry | Covariant, contravariant tensors, invariants, tensors and relativity | T1 and R2:  Chapter 1,2,3,4 ,  Notes |
| 35-40 | Special Functions | Legendre, Bessel and Hernite polynomials, Complete basis formation using them, Transformation from one basis to  another | T1, T2  and Notes |

# Evaluation Scheme:

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **EC**  **No.** | **Component** | **Duration** | | **Weighta ge**  **(%)** | **Date & time** | **Nature** |
| 1 | Mid Sem Exam | 1.5 hrs | 30 | | 13/03 11.30 - 1.00PM | Closed Book |
| 2 | Quiz |  | 30 | |  | Closed Book |
| 3 | Comprehensive  exam | 3 hours | 40 | | 08/05 AN | Open Book |

**Chamber Consultation Hours:** To be announced in the class.

es

**Notices:** Will be displayed on the Physics department notice board and in CMS.

**Make-up Policy:** Make-up will be given only in genuine cases, that is, illness leading to hospitalization or going out of station with prior permission. No make-ups for the surprise tests.

**Academic Honesty and Integrity Policy:**

Academic honesty and integrity are to be maintained by all the students throughout the semester and no type of academic dishonesty is acceptable.

# Instructor-in-charge

**PHY F243**